

```
In[1]:= (* Escenario 1: Estado puramente leucémico,
evolución al cabo de un año. Lento
decrecimiento de los compartimientos sanos pero rápido
crecimiento de los compartimientos leucémicos *)
```

```
b = ParametricNDSolve [{x'[t] ==
  ((2*a1c)/(1+1.6*(10^-11)*y[t]+1.6*(10^-11)*m[t])-1)*
  p1c*x[t]-d1c*x[t],
y'[t]==2*(1-a1c/(1+1.6*(10^-11)*y[t]+1.6*(10^-11)*m[t]))*
  p1c*x[t]-d2c*y[t],
l'[t]==((2*a1l)/(1+1.6*(10^-11)*y[t]+1.6*(10^-11)*m[t])-1)*
  p1l*l[t]-d1l*l[t],
m'[t]==2*(1-a1l/(1+1.6*(10^-11)*y[t]+1.6*(10^-11)*m[t]))*
  p1l*l[t]-d2l*m[t],x[0]==6.25*10^7,
y[0]==6.25*10^9,l[0]==10,m[0]==0},{x,y,l,m},
{t,365},{a1c,p1c,d1c,d2c,a1l,p1l,d1l,d2l}]
```

Out[1]= $\left\{ x \rightarrow \text{ParametricFunction} \left[\begin{array}{c} \text{+} \\ \text{M} \end{array} \right] \text{ Expression: } x \text{ Parameters: } \{a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l\} \right\},$

$y \rightarrow \text{ParametricFunction} \left[\begin{array}{c} \text{+} \\ \text{M} \end{array} \right] \text{ Expression: } y \text{ Parameters: } \{a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l\}$

$l \rightarrow \text{ParametricFunction} \left[\begin{array}{c} \text{+} \\ \text{M} \end{array} \right] \text{ Expression: } l \text{ Parameters: } \{a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l\}$

$m \rightarrow \text{ParametricFunction} \left[\begin{array}{c} \text{+} \\ \text{M} \end{array} \right] \text{ Expression: } m \text{ Parameters: } \{a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l\}$

```
In[2]:= x1=x[0.55,1,0,0.01,0.57,0.5,0,0.1]/.b
y1=y[0.55,1,0,0.01,0.57,0.5,0,0.1]/.b
l1=l[0.55,1,0,0.01,0.57,0.5,0,0.1]/.b
m1=m[0.55,1,0,0.01,0.57,0.5,0,0.1]/.b
```

Out[2]= InterpolatingFunction[$\left[\begin{array}{c} \text{+} \\ \text{C} \end{array} \right]$ Domain: {{0., 365.}} Output: scalar]

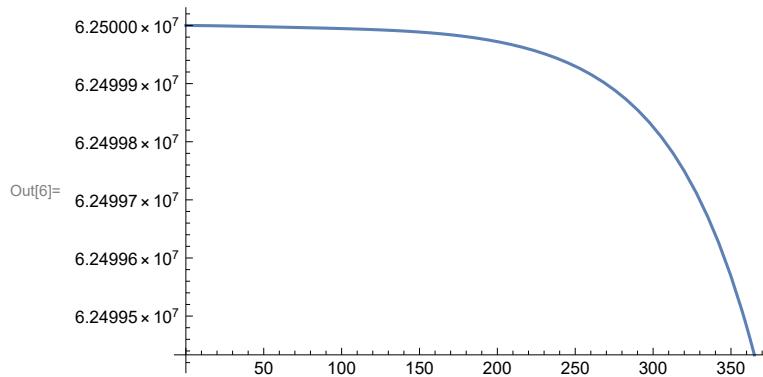
Out[3]= InterpolatingFunction[$\left[\begin{array}{c} \text{+} \\ \text{C} \end{array} \right]$ Domain: {{0., 365.}} Output: scalar]

Out[4]= InterpolatingFunction[$\left[\begin{array}{c} \text{+} \\ \text{C} \end{array} \right]$ Domain: {{0., 365.}} Output: scalar]

Out[5]= InterpolatingFunction[$\left[\begin{array}{c} \text{+} \\ \text{C} \end{array} \right]$ Domain: {{0., 365.}} Output: scalar]

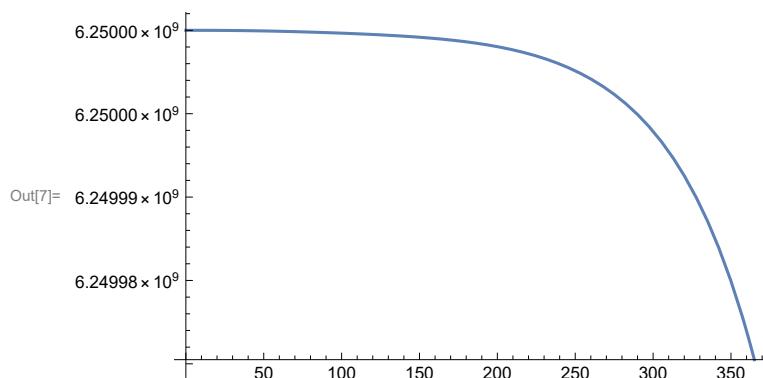
```
In[6]:= Plot[x1[t], {t, 0., 365}]
```

representación gráfica



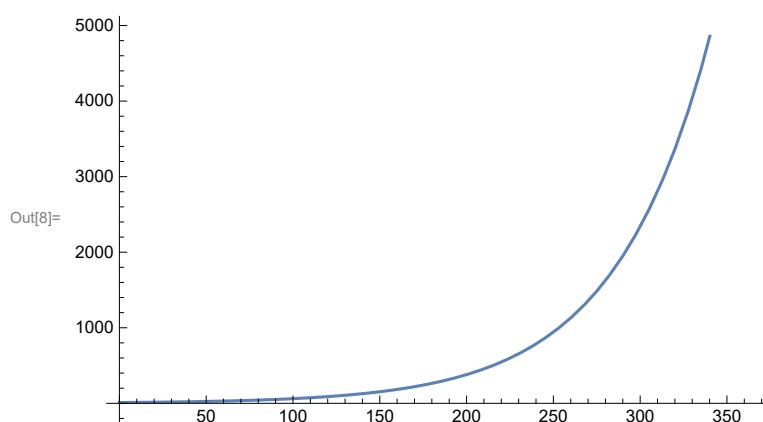
```
In[7]:= Plot[y1[t], {t, 0., 365}]
```

representación gráfica



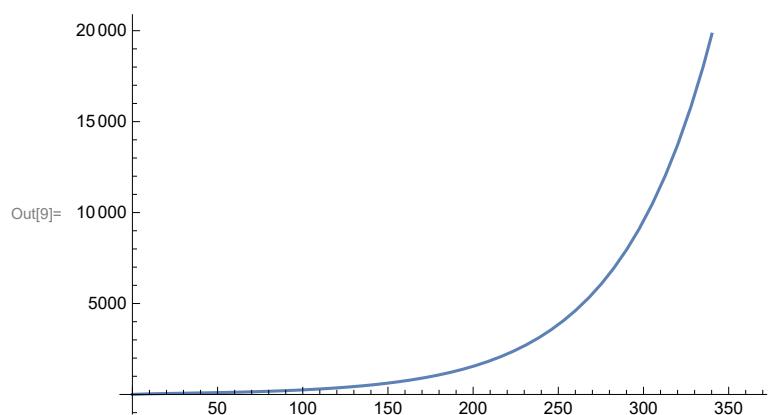
```
In[8]:= Plot[l1[t], {t, 0., 365}]
```

representación gráfica



```
In[9]:= Plot[m1[t], {t, 0., 365}]
```

representación gráfica



In[10]:= (* Escenario 2: Extinción de la población de células leucémicas y restablecimiento del equilibrio saludable: Estabilidad del estado de equilibrio saludable.*)

```
bb = ParametricNDSolve [
  resolvedor diferencial numérico paramétrico
  {x'[t] == (2*a1c / (1 + 1.6*(10^-11)*y[t] + 1.6*(10^-11)*m[t]) - 1) *
    p1c*x[t] - d1c*x[t],
   y'[t] == 2*(1 - (a1c / (1 + 1.6*(10^-11)*y[t] + 1.6*(10^-11)*m[t]))) *
    p1c*x[t] - d2c*y[t],
   l'[t] == (2*a1l / (1 + 1.6*(10^-11)*y[t] + 1.6*(10^-11)*m[t]) - 1) *
    p1l*l[t] - d1l*l[t],
   m'[t] == 2*(1 - (a1l / (1 + 1.6*(10^-11)*y[t] + 1.6*(10^-11)*m[t]))) *
    p1l*l[t] - d2l*m[t], x[0] == 6.25*10^7,
   y[0] == 6.25*10^9, l[0] == 10, m[0] == 0}, {x, y, l, m},
  {t, 730}, {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}]
```

Out[10]= {x → ParametricFunction [ Expression: x Parameters: {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}] ,

y → ParametricFunction [ Expression: y Parameters: {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}] ,

l → ParametricFunction [ Expression: l Parameters: {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}] ,

m → ParametricFunction [ Expression: m Parameters: {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}] }

```
In[11]:= x1 = x[0.55, 1, 0, 0.01, 0.53, 1.5, 0, 0.1] /. bb
y1 = y[0.55, 1, 0, 0.01, 0.53, 1.5, 0, 0.1] /. bb
l1 = l[0.55, 1, 0, 0.01, 0.53, 1.5, 0, 0.1] /. bb
m1 = m[0.55, 1, 0, 0.01, 0.53, 1.5, 0, 0.1] /. bb
```

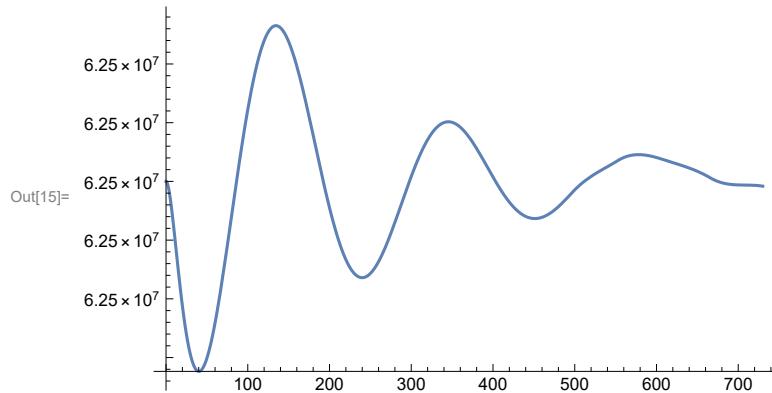
Out[11]= InterpolatingFunction[ Domain: {{0., 730.}}]
Output: scalar

Out[12]= InterpolatingFunction[ Domain: {{0., 730.}}]
Output: scalar

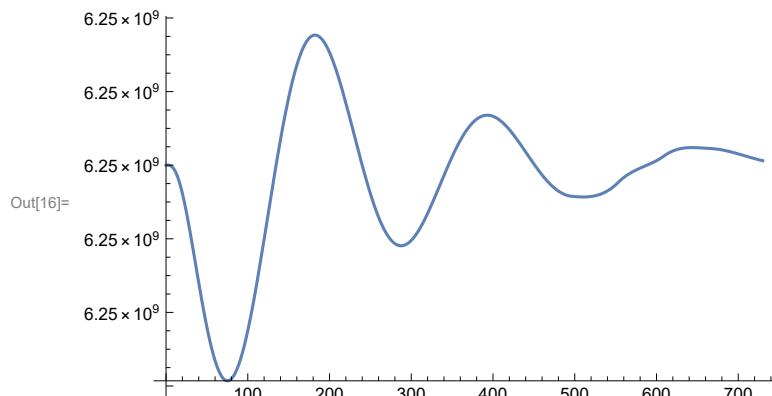
Out[13]= InterpolatingFunction[ Domain: {{0., 730.}}]
Output: scalar

Out[14]= InterpolatingFunction[ Domain: {{0., 730.}}]
Output: scalar

```
In[15]:= Plot[x1[t], {t, 0., 730.}]
representación gráfica
```

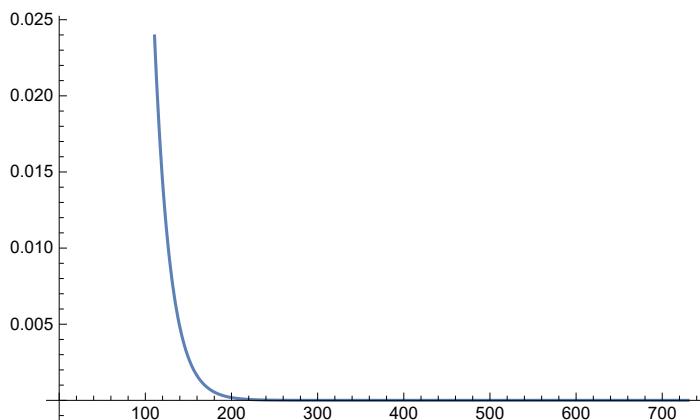


```
In[16]:= Plot[y1[t], {t, 0., 730.}]
representación gráfica
```



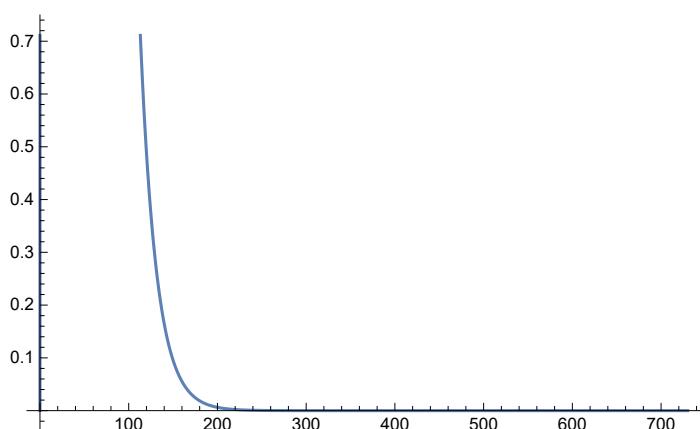
```
In[17]:= Plot[l1[t], {t, 0., 730.}]
```

[representación gráfica]



```
In[18]:= Plot[m1[t], {t, 0., 730.}]
```

[representación gráfica]



(*Escenario 3:

Equilibrio con la coexistencia de células sanas y leucémicas:
el recuento de células leucémicas está en el orden
de magnitud del recuento de células maduras sanas. *)

```
In[19]:= bbb = ParametricNDSolve [{x'[t] ==  
  ((2*a1c) / (1 + 1.6*(10^-11)*y[t] + 1.6*(10^-11)*m[t]) - 1) *  
   p1c*x[t] - d1c*x[t],  
  y'[t] == 2*(1 - a1c / (1 + 1.6*(10^-11)*y[t] + 1.6*(10^-11)*m[t])) *  
   p1c*x[t] - d2c*y[t],  
  l'[t] == ((2*a1l) / (1 + 1.6*(10^-11)*y[t] + 1.6*(10^-11)*m[t]) -  
   1) * p1l*l[t] - d1l*l[t],  
  m'[t] == 2*(1 - a1l / (1 + 1.6*(10^-11)*y[t] + 1.6*(10^-11)*m[t])) *  
   p1l*l[t] - d2l*m[t], x[0] == 6.25*10^7,  
  y[0] == 6.25*10^9, l[0] == 100, m[0] == 0}, {x, y, l, m},  
 {t, 730}, {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}]
```

Out[19]= $\{x \rightarrow \text{ParametricFunction}[\text{Expression: } x, \text{Parameters: } \{a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l\}],$

$y \rightarrow \text{ParametricFunction}[\text{Expression: } y, \text{Parameters: } \{a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l\}]$,

$l \rightarrow \text{ParametricFunction}[\text{Expression: } l, \text{Parameters: } \{a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l\}]$,

$m \rightarrow \text{ParametricFunction}[\text{Expression: } m, \text{Parameters: } \{a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l\}] \}$

```
In[20]:= x1 = x[0.55, 1, 0, 0.01, 0.55, 2.5, 0, 0.00001] /. bbb  
y1 = y[0.55, 1, 0, 0.01, 0.55, 2.5, 0, 0.00001] /. bbb  
l1 = l[0.55, 1, 0, 0.01, 0.55, 2.5, 0, 0.00001] /. bbb  
m1 = m[0.55, 1, 0, 0.01, 0.55, 2.5, 0, 0.00001] /. bbb
```

Out[20]= InterpolatingFunction[ Domain: {{0., 730.}} Output: scalar]

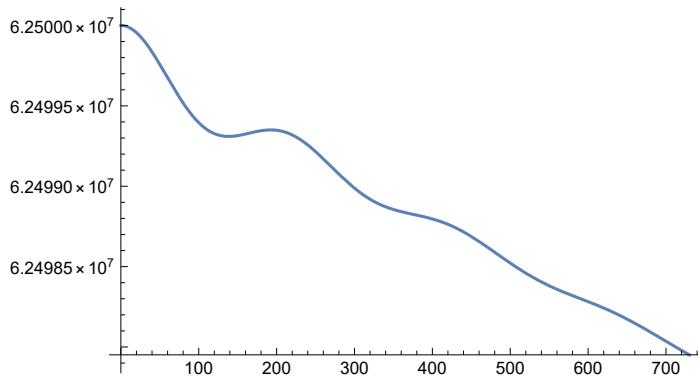
Out[21]= InterpolatingFunction[ Domain: {{0., 730.}} Output: scalar]

Out[22]= InterpolatingFunction[ Domain: {{0., 730.}} Output: scalar]

Out[23]= InterpolatingFunction[ Domain: {{0., 730.}} Output: scalar]

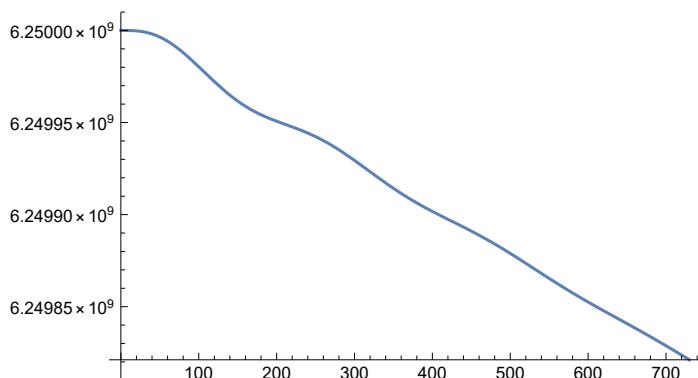
```
In[24]:= Plot[x1[t], {t, 0., 730.}]
```

representación gráfica



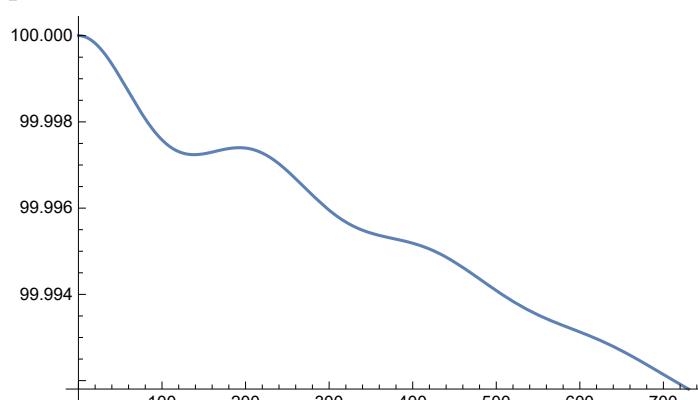
```
In[25]:= Plot[y1[t], {t, 0., 730.}]
```

representación gráfica



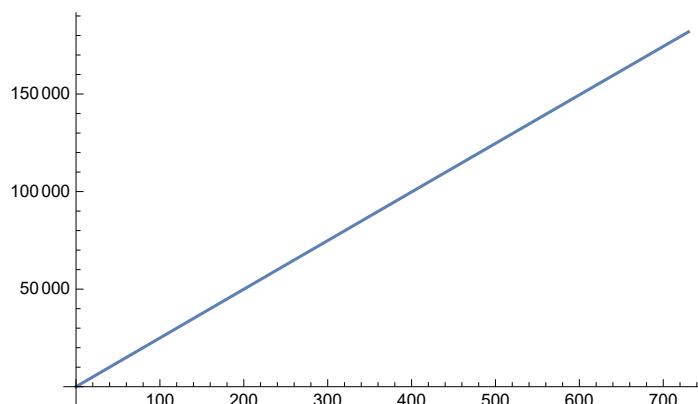
```
In[26]:= Plot[l1[t], {t, 0., 730.}]
```

representación gráfica



In[27]:= Plot[m1[t], {t, 0., 730.}]

representación gráfica



Out[27]=

(* Escenario 4:

Equilibrio con la coexistencia de células sanas y leucémicas:
el recuento de células leucémicas es pequeño
y el cambio de recuentos de células sanas es
invisible en una escala clínicamente relevante.*)

```
In[28]:= bbbb = ParametricNDSolve [{x'[t] ==
  resolvedor diferencial numérico paramétrico
  ((2 * a1c) / (1 + 1.6 * (10^-11) * y[t] + 1.6 * (10^-11) * m[t]) - 1) *
  p1c * x[t] - d1c * x[t],
  y'[t] == 2 * (1 - a1c / (1 + 1.6 * (10^-11) * y[t] + 1.6 * (10^-11) * m[t])) *
  p1c * x[t] - d2c * y[t],
  l'[t] == ((2 * a1l) / (1 + 1.6 * (10^-11) * y[t] + 1.6 * (10^-11) * m[t]) -
  1) * p1l * l[t] - d1l * l[t],
  m'[t] == 2 * (1 - a1l / (1 + 1.6 * (10^-11) * y[t] + 1.6 * (10^-11) * m[t])) *
  p1l * l[t] - d2l * m[t], x[0] == 6.25 * 10^7,
  y[0] == 6.25 * 10^9, l[0] == 10, m[0] == 0}, {x, y, l, m},
  {t, 730}, {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}]
```

Out[28]= {x → ParametricFunction [Expression: x Parameters: {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}] ,

y → ParametricFunction [Expression: y Parameters: {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}] ,

l → ParametricFunction [Expression: l Parameters: {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}] ,

m → ParametricFunction [Expression: m Parameters: {a1c, p1c, d1c, d2c, a1l, p1l, d1l, d2l}] }

```
In[29]:= x1 = x[0.55, 1, 0, 0.01, 0.55, 0.5, 0, 0.1] /. bbbb
y1 = y[0.55, 1, 0, 0.01, 0.55, 0.5, 0, 0.1] /. bbbb
l1 = l[0.55, 1, 0, 0.01, 0.55, 0.5, 0, 0.1] /. bbbb
m1 = m[0.55, 1, 0, 0.01, 0.55, 0.5, 0, 0.1] /. bbbb
```

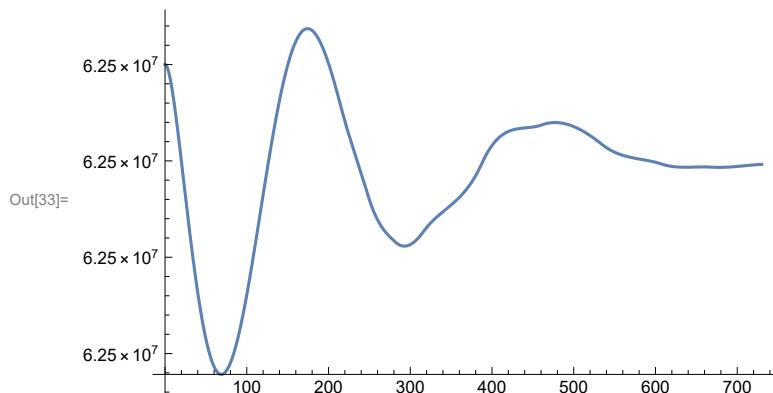
Out[29]= InterpolatingFunction[ Domain: {{0., 730.}}]
Output: scalar

Out[30]= InterpolatingFunction[ Domain: {{0., 730.}}]
Output: scalar

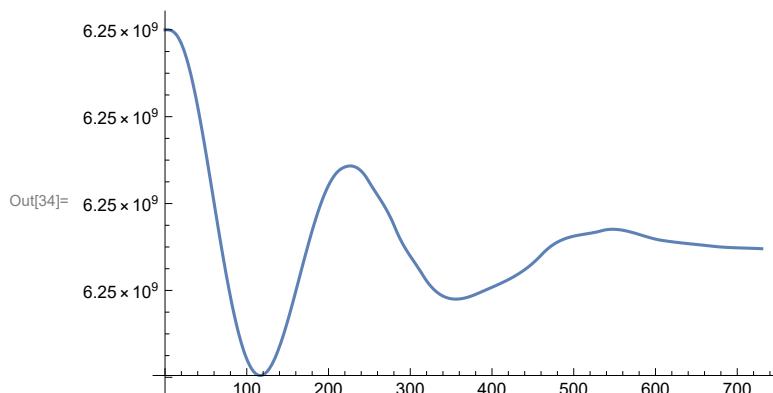
Out[31]= InterpolatingFunction[ Domain: {{0., 730.}}]
Output: scalar

Out[32]= InterpolatingFunction[ Domain: {{0., 730.}}]
Output: scalar

```
In[33]:= Plot[x1[t], {t, 0., 730.}]
representación gráfica
```

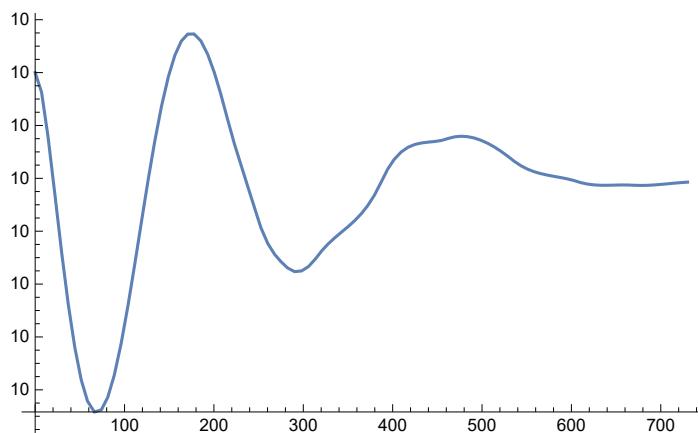


```
In[34]:= Plot[y1[t], {t, 0., 730.}]
representación gráfica
```



In[35]:= Plot[l1[t], {t, 0., 730.}]

| representación gráfica



In[36]:= Plot[m1[t], {t, 0., 730.}]

| representación gráfica

